### DYNAMICS AND STRUCTURE OF GALAXIES GALACTIC ASTRONOMY

# 2.2 Local Kinematics

### OVERVIEW

- Aim of the following classes
- Solar neighborhood & disk structure
- Distance measurements
- Velocities of nearby stars
- Frames of reference
- Local kinematics

### AIM

- Going from the small scale to the large scale of the Galaxy
- Acquire observational data to build the picture of the formation of the Galaxy (not give it for granted)

NOTE: In astronomy, Galaxy, with "G" always refers to the Milky Way, while galaxy refers to a general galaxy (the title of this class is ambiguous!)

### 1 - SOLAR NEIGHBORHOOD AND DISK STRUCTURE

- "Neighborhood" vary according to the context
   (~200-300 pc, where the dust limits observations)
- Components of the Milky Way (see previous classes):



# THE SOLAR NEIGHBORHOOD – MASS CONTENT

#### • Stars

differences:

- Initial Mass Function (IMF)
- stellar evolution

Tipo	Densidad [M <sub>o</sub> pc <sup>-3</sup> ]
Estrellas de SP O-F	0.014
Estrellas de SP G-M	0.036
Estrellas del halo	0.0001
Enanas blancas	0.005
Total	0.055

- Interstellar medium (ISM) ~ 0.04 M\_sun/pc^3 (gas and dust)
- Dark matter ~ 0.01 M\_sun/pc^3

```
=> TOTAL ~ 0.1 M_sun/pc^3
```

# THE SOLAR NEIGHBORHOOD – VERTICAL DISTRIBUTION

#### • Stars

- exponential

$$n(z) = n_0 e^{-|z|/z_0}$$
.

	2
Тіро	$z_{\theta}$ (pc)
O-B	50
А	120
F	190
dG	340
dK	350
dM	350

depends on stellar

class

- Interstellar medium (ISM) thin disk (gas and dust)
- Dark matter spherical halo

# THE SOLAR NEIGHBORHOOD – VERTICAL DISTRIBUTION

#### • Stars

exponential

$$n(z) = n_0 e^{-|z|/z_0}.$$

depends on stellar

class

- Interstellar medium (ISM) h ~50 pc (gas and dust)
- Dark matter spherical halo

	~
Тіро	<i>z</i> <sub>θ</sub> (pc)
O-B	50
А	120
F	190
dG	340
dK	350
dM	350



# THE SOLAR NEIGHBORHOOD – DISK (VERTICAL SCALE)

More hints about disk evolution:

- The double profile of the disk
  - thin disk (h~250 pc) (95% of stars)
  - thick disk (h~1000 pc)
- Metallicity:
  - thin disk <[Fe/H]>  $\sim$  -0.3
  - thick disk <[Fe/H]>  $\sim$  -0.6





#### thin disk:

- hosts younger stars
- Same h as the gas
- narrower (as the name says)
- metal richer

## THE SOLAR NEIGHBORHOOD – DISK EVOLUTION

Possible disk evolution:

- Stars are born in the same place (where is the gas), but their obits evolve in via interactions with gas clouds and spiral arms
  - → interactions not sufficient to "puff-up" thick disk to 1 kpc (?)
- Old galaxy interaction "heated" ALL the thin disk, and later the gas fell back to the plane, where young stars now form
  - $\rightarrow$  gas relaxes faster than stars because of viscosity

# THE SOLAR NEIGHBORHOOD – CAVEATS ABOUT DISK EVOLUTION

Keep in mind:

- thick/thin disks are commonly found in spiral galaxies
   e.g. Yoachim (2005; arXiv:astro-ph/0508460v1)
- the separation thick/thin might be artificial: it could be a series of components e.g. Bovy (2012, ApJ, 753, 148)

### 2 – DISTANCE MEASUREMENTS

Distance measurement for the local stars

• Parallax (trigonometric):

 $d(pc) = \frac{1AU}{\pi(\text{''})}$ 

Hipparchos (1989 – 1993) Gaia (first data release 2017)



	Hipparchos	Gaia
mag limit (V)	12	20
Effective distance	1 kpc	10 Mpc
Observed objects	~10^5	~10^9
Distance accuracy	~5-10%	<1%

### SPECTROSCOPIC PARALLAX

- Parallax (spectroscopic):
  - for a given spectral class we know L
  - compare L (model) VS F (observed)
  - $\rightarrow$  find distance:

 $L = 4\pi d^2 F$ 



- Features:
  - less accurate than trigonometric parallax
  - valid up to larger (pre-Gaia era) distances (~100 kpc)
  - affected by dust absorption
  - luminosity class difficult to disentangle for distant stars

### OTHER STELLAR DISTANCE MEASUREMENTS

- Stellar peculiar characteristics:
  - Cepheids (supergiants):
    - L Period



- RR Lyrae (horizontal branch)
 spectroscopic parallax
 (they have an extremely constant L)

### 3 - VELOCITIES OF NEARBY STARS

- Proper motion  $\mu$  [rad/sec] = motion of an object in the sky
- ... but 3D velocity v has more components:
  - tangential component (proper motion)
  - radial component (doppler)



• In galactic coordinates, v\_t can be further projected as:



# VELOCITIES OF NEARBY STARS -HELIOCENTRIC CARTESIAN SYSTEM

• Switching to the "comfortable" heliocentric Cartesian system:



$$W = \frac{dz}{dt} = r\sin b + r\dot{b}\cos b$$

From previous slide:

 $r = v_r$   $r \dot{l} \cos b = v_l$   $r \dot{b} = v_b$ 

 $U = v_r \cos b \cos l - v_b \sin b \cos l - v_l \sin l$  $V = v_r \cos b \sin l - v_b \sin b \sin l + v_l \cos l$  $W = v_r \sin b + v_b \cos b$ 

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• Switching to the "comfortable" heliocentric Cartesian system:



### VELOCITIES OF NEARBY STARS -HELIOCENTRIC CARTESIAN SYSTEM

 $\upsilon_r = U \cos b \cos l + V \cos b \sin l + W \sin b$  $\upsilon_b = -U \sin b \cos l - V \sin b \sin l + W \cos b$  $\upsilon_l = U \sin l + V \cos l$ 

Reverse (we will need them later)

 $U = v_r \cos b \cos l - v_b \sin b \cos l - v_l \sin l$  $V = v_r \cos b \sin l - v_b \sin b \sin l + v_l \cos l$  $W = v_r \sin b + v_b \cos b$ 

### 4 – FRAMES OF REFERENCE

• Galacto-centic system is the natural system (!= galactic coordinates!):



 However, to study the Sun's neighborhood is more convenient to adopt a "local" frame of reference:



### 4 – FRAMES OF REFERENCE

IF stars were really on perfectly circular orbits

#### Local Standard of Rest (LSR)

#### Kinematic LSR

heliocentric, rotates at the

average velocity of local stars

(no assumptions on why)



#### **Dynamic LSR**

defined at any point, rotates on

circular orbit with a velocity  $\Theta_0$ 

imposed by axisymmetric potential

### PECULIAR VELOCITY

• **Peculiar velocity** = velocity (u,v,w) of a star w/r to its dyn. LSR (LSR\*)

Variable	Descripción	Z	
<i>X,Y,Z</i>	Coordenadas de un objeto en el SFR		
П,Ө,Ζ	Velocidad de un objeto en el SFR	$\Pi = dR/dt$	
(0, <b>O</b> <sub>0</sub> ,0)	Velocidad del LSR en el SFR	$\Omega = D d\Omega/dt$ Star	
и, v, w	Velocidad peculiar, i.e., velocidad de una	$\Theta \equiv K d\theta/dt$ z –	Rotation
	estrella respecto a sus SLR.	Z = dz/dt	
U,V,W	Velocidad de un objeto respecto al Sol	Sun	· Galactic center
$v_{\Theta}'$	Velocidad acimutal del Sol respecto al LSR		
	cinemático		
v <sub>e</sub>	Velocidad acimutal del Sol respecto al LSR		
	dinámico	$u_* = 11_* - 11_{SLR} = 11$	
$\mathcal{U}_r$	Velocidad de un objeto respecto al Sol, a lo	5.5.1	Peculiar
	largo de la visual	$v_* = \Theta_* - \Theta_{ISP} = \Theta - \Theta_0$	
$\boldsymbol{v}_l$ , $\boldsymbol{v}_b$	Velocidad de un ojbeto respecto al Sol, en	LSR 0	velocity
	dirección l, b, respectivamente	$W_* = Z_* - Z_{ISR} = Z$	velocity

- To convert this to heliocentric coordinates we need to:
  - $\rightarrow$  find the peculiar velocity of Sun w/r to its LSR (LSR\_sun)
  - $\rightarrow$  find the differential velocity between LSR\_sun and LSR\*

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  - $\rightarrow$  find the peculiar velocity of Sun w/r to its LSR (LSR\_sun)
  - → find the differential velocity between LSR\_sun and LSR\*

(we ignore this assuming no differential rotation – nearby stars)

# PECULIAR VELOCITY – HELIOCENTRIC COORDINATES

• Velocity of a star w/r to the Sun:

$$U_{*} = u_{*} - u_{\Theta} - (\Pi_{LSR^{*}} - \Pi_{LSR\Theta})$$
  

$$V_{*} = v_{*} - v_{\Theta} - (\Theta_{LSR^{*}} - \Theta_{LSR\Theta})$$
  

$$W_{*} = w_{*} - w_{\Theta} - (Z_{LSR^{*}} - Z_{LSR\Theta})$$
  

$$U_{*} = u_{*} - u_{\Theta} = \Pi_{*} - \Pi_{\Theta}$$
  

$$V_{*} = v_{*} - v_{\Theta} = \Theta_{*} - \Theta_{\Theta}$$
  

$$W_{*} = w_{*} - w_{\Theta} = Z_{*} - Z_{\Theta}$$
  

$$W_{\Theta} = W_{\Theta} \otimes USR_{sun}$$
  

$$W_{\Theta} \otimes USR_{sun}$$

• Adopting a sample of nearby stars, we can say:

$$\langle U_* \rangle = \langle u_* \overline{\rangle}^{-} u_{\Theta} = -u_{\Theta}$$
$$\langle W_* \rangle = \langle w_* \rangle - w_{\Theta} = -w_{\Theta}$$

- But we cannot say:  $\langle v_* 
  angle = 0$ 
  - that is true in the kinematic LSR (actually it's the definition)
  - ... but now we are using the dynamic LSR

### ESTIMATING <v\*>

- A = Sun's orbit
  - B = random star orbit
  - C = circle around Galaxy center

(where LSR is defined)



• Consider that stars passing near the Sun when it is at the apocenter:



- are slower

C

- come from the outskirts of the Galaxy

(where density is lower)

 $\rightarrow$  on average stars are slower than the Sun!

Asymmetric drift  $\rightarrow \langle v^* \rangle < 0$ 

We will therefore write:  $\langle V_* \rangle = \langle v_* \rangle - v_{\Theta}$ and define the velocity of Sun w/r to the kinematic LSR  $v_{\Theta}'$ :  $v_{\Theta}' = -\langle V_* \rangle$ 

## FORMULATION OF PECULIAR MOTION OF THE SUN

Finally, the peculiar motion (u, v, w) of the Sun (in dyn. LSR\_sun) is:

$$\begin{split} u_{\Theta} &= -\langle U_{*} \rangle \\ v_{\Theta} &= -\langle V_{*} \rangle + \langle v_{*} \rangle = v_{\Theta}^{'} + \langle v_{*} \rangle \\ w_{\Theta} &= -\langle W_{*} \rangle \end{split}$$

- while  $(u_0, v'_0, w_0)$  defines the motion of the Sun in the kin. LSR
- Let's now see how to measure it:

 $\upsilon_r = U \cos b \cos l + V \cos b \sin l + W \sin b$  $\upsilon_b = -U \sin b \cos l - V \sin b \sin l + W \cos b$  $\upsilon_l = U \sin l + V \cos l$ 

Star velocity w/r Cartesian heliocentric (seen previously) for each star i in a sample:  $v_{ri} = U_i \cos l_i \cos b_i + V_i \sin l_i \cdot \cos b_i + W_i \sin b_i$ By grouping stars in sub-samples with (l,b) ~ CONST :

$$\upsilon_{ri} = \alpha U_i + \beta V_i + \gamma W_i$$

$$\langle \upsilon_{ri} \rangle = -\alpha \cdot u_{\Theta} - \beta \cdot v_{\Theta} - \gamma \cdot w_{\Theta}$$

### MEASUREMENT OF PECULIAR MOTION OF THE SUN

$$\langle \upsilon_{ri} \rangle = -\alpha \cdot u_{\Theta} - \beta \cdot v_{\Theta} - \gamma \cdot w_{\Theta}$$

- This equation holds for each sub-sample (1,b)  $\sim$  CONST
  - $\rightarrow$  for M sub-samples (j = 1 ... M), we have M equations of the type:

$$\alpha_{j}u_{\Theta} + \beta_{j}v_{\Theta}' + \gamma_{j}w_{\Theta} = k_{j}$$

- Solving the equations (3 sub-samples are sufficient)
  - $\rightarrow$  we obtain the (u<sub>0</sub>, v'<sub>0</sub>, w<sub>0</sub>) motion of the Sun in the kinematic LSR



 $\rightarrow$  we can now obtain the motion of any star

Values measured:

Sun is moving

north and inward,

faster than LSR\_sun

 $u_{\Theta} = 10.0 \quad km \cdot s^{-1}$  $v_{\Theta}' = 5.2 \quad km \cdot s^{-1}$  $w_{\Theta} = 7.2 \quad km \cdot s^{-1}$ 

## MEASUREMENT OF PECULIAR MOTION OF THE SUN

• Let's switch to the  $(u_0, v_0, w_0)$  motion of the Sun in the dynamic LSR (i.e., let's find  $v_0$ )



• We can assume that  $v_{\theta}$  depends on how many elliptical obits there are Observationally, this is given by the dispersion on radial velocities  $\Pi$ :

$$\langle v_* 
angle \sim < \Pi^2 >$$

### MEASUREMENT OF PECULIAR MOTION OF THE SUN



# MOTION OF THE LSR\_sun IN THE GALAXY (SFR)

- We can use the apparent movement of the radio source SgrA\* (AGN)
- Radio interferometry (e.g. VLBI) can achieve high (µarcsec) resolution
- Assuming  $R_0 = 8.5 \text{ kpc}$ 
  - $\rightarrow$  relative velocity  $\Theta_0 \sim 235$  km/sec
- Can repeat with any non-rotating object:
  - halo GCs  $\rightarrow \Theta_0 \sim 220$  km/sec
  - other galaxies (big uncertainties)



### 5 – LOCAL KINEMATICS -DISK

- Distribution of stellar velocity around u, v, w  $\sim$  Gaussian
- The distribution changes with:
  - the axis u, v, w
  - the stellar type

Tipo	$< u^2 > 0.5$	$< v^2 > 0.5$	$<_W^2>^{0.5}$	<i>l</i> <sub>v</sub> (°)
Enanas				
B0	10	9	6	-50
A0	15	9	9	15
F0	24	13	10	19
G0	26	18	15	21
K0	28	16	11	2
M0	32	21	10	3
Gigantes				
A	22	13	9	27
F	28	15	9	14
G	26	18	15	12
K0	31	21	16	14
Súpergigantes				
Cefeidas	13	9	5	-
O-B5	12	11	9	36



# LOCAL DISK KINEMATICS - VELOCITY DISTRIBUTIONS

- We observe:
  - distribution is tighter for more massive (younger) stars
  - later stellar types along M-S include stars of a wider range of ages

(hence their distributions are intrinsically wider)

- Consistent with the picture that stars form in the gas disk, with:
  - small vertical separation
  - similar peculiar velocities
- ... and their obits evolve by interactions with molecular clouds and spiral arms NOTE: still not enough to create thick disk!

# LOCAL DISK KINEMATICS -VELOCITY DISTRIBUTIONS 2D

- Distribution around u, w  $\sim$  symmetric
- Distribution around v !~ symmetric and <v> < 0 (asymmetric drift)</li>
- Alternative view:





# LOCAL DISK KINEMATICS -VELOCITY DISTRIBUTIONS 2D

- dispersion u > dispersion v > dispersion w (why? under debate)
- smaller mass ↔ higher dispersion
- dispersion v asymmetric,  $\langle v \rangle < 0$



# LOCAL DISK KINEMATICS -VELOCITY ELLIPSOID

#### Co-moving groups

- can be identified on the u, v, w hyperplane (see e.g. work of A. Binks)
- mostly composed by massive (young) stars

(they get dispersed by interactions)



Examples:

Pleiads, Hyades, Sirio group

• We define:

- the velocity ellipsoid (it's 3D)
- the vertex deviation (angle l\_v)

# LOCAL DISK KINEMATICS -VELOCITY ELLIPSOID

How to write the velocity Probability distribution Function P(V)?
 If the distributions were independent & symmetric Gaussians:

$$P(V) = P_u(u)P_v(v)P_w(w)$$
$$= \frac{1}{(2\pi)^{1.5}\sigma_u\sigma_v\sigma_w} \exp\left[-\left(\frac{u^2}{2\sigma_u^2} + \frac{v^2}{2\sigma_v^2} + \frac{w^2}{2\sigma_w^2}\right)\right]$$

... but the only symmetric Gaussian is w, while u and v are correlated !

• We choose new axis set: •  $\mathbf{u_1} \leftarrow \text{rotating } \mathbf{u}, \mathbf{v} \text{ by } \mathbf{l_v}$ •  $\mathbf{v_2}$ •  $\mathbf{w} \leftarrow \text{we keep this axis}$   $\frac{1}{(2\pi)^{1.5}\sigma_1\sigma_2\sigma_w} \exp\left[-\left(\frac{u_1^2}{2\sigma_1^2} + \frac{v_2^2}{2\sigma_2^2} + \frac{w^2}{2\sigma_w^2}\right)\right]$ Schwarzschild distribution (somebody call this "velocity ellipsoid")

# LOCAL DISK KINEMATICS -VERTEX DEVIATION

- Considerations on vertex deviation:
  - 1- is more significant for younger stars
  - 2- in an axi-symmetric system, u would be a principal axis

Tipo	$< u^2 > 0.5$	$< v^2 > 0.5$	$< W^2 > 0.5$	$l_{\rm v}$ (°)
Enanas				
B0	10	9	6	-50
A0	15	9	9	15
F0	24	13	10	19
G0	26	18	15	21
K0	28	16	11	2
M0	32	21	10	3
Gigantes				
A	22	13	9	27
F	28	15	9	14
G	26	18	15	12
K0	31	21	16	14
Súpergigantes				
Cefeidas	13	9	5	-
O-B5	12	11	9	36

- Possible origins of vertex deviation:

   initial formation condition
   few nearby co-moving groups strongly
   influence the (u,v) distribution
   (stochastic occurrence)
  - 2- local potential is **not** axi-symmetric attraction by e.g. spiral arms

### LOCAL HALO KINEMATICS

- Characteristics of halo stars:
  - large peculiar velocities (i.e. velocity w/r to their LSR)
    - → a.k.a. high-velocity stars
  - large asymmetric drift (i.e. <v\*>)
    - $\rightarrow$  large difference w/r to a circular orbit

(halo is a sphere with almost no rotation)

• For halo, better use the Galcto-centric (SFR) velocities ( $\Pi$ ,  $\Theta$ , Z)

	Tipo	$<\!\Theta\!\!>\!\!-\Theta_0$	< 0>	$\sigma_{\Pi}$	$\sigma_{\Theta}$	$\sigma_{Z}$	Calacta
	Cúmulos	-165	55	145	-	-	Galacio-
LSR sun	globulares						centric
-	Sub-enanas	-185	35	170	90	65	
	RR Lyraes	-220	0	210	120	90	(SFR)

( $\Theta_0$  = velocity of LSR\_sun in the SFR) ~ 220 km/sec

### LOCAL HALO KINEMATICS

#### • Additionally:

- large velocity dispersions ( $\sigma_{\Pi}$ ,  $\sigma_{\Theta}$ ,  $\sigma_{Z}$ )
- milder rotation than disk (< $\Theta$ >)

inner halo  $\rightarrow$  prograde 0÷60 km/sec

outer halo  $\rightarrow$  retrograde -40÷-70 km/sec

Frank & White (1980), Carollo (2007, Nature, 450, 1020)

#### • We will also see that halo stars are:

- old
- metal poor

Tipo	$<\!\!\Theta\!\!>$ - $\!\Theta_0$	$<\!\!\Theta\!\!>$	$\sigma_{\Pi}$	$\sigma_{\Theta}$	$\sigma_{Z}$
Cúmulos	-165	55	145	-	-
globulares					
Sub-enanas	-185	35	170	90	65
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### KINEMATICS – BIG PICTURE

